



# Geoid and MDT of the Arctic Ocean

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## Outline:

- Determination of MDT from remote sensing (geoid+altimetry) in ice-covered areas – *what can remote sensing do?*
- MDT estimate in Arctic Ocean from ICESat /ERS and GRACE/ArcGP
- Comparison to oceanographic models..





## The problem in the Arctic Ocean: Sea-ice, geoid, MSS and MDT ...

Basic equation and challenge:

$$MDT = h - N - T - F$$

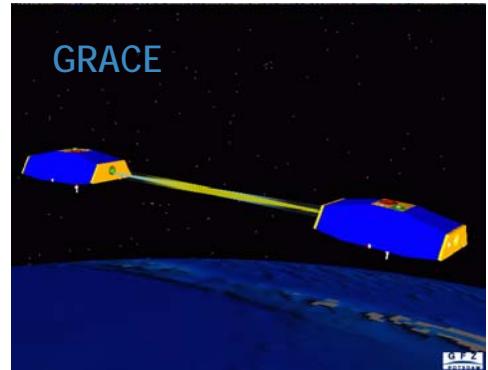
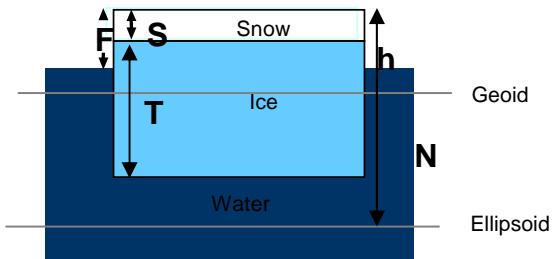
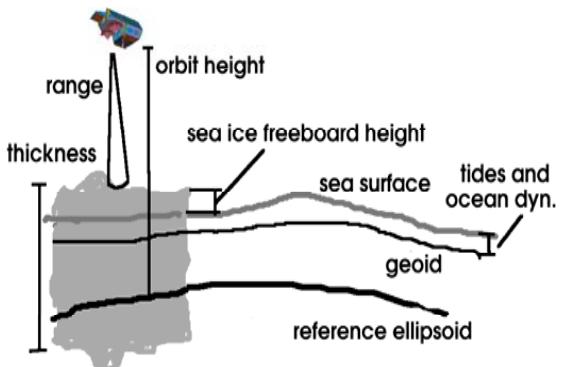
h: Ellipsoidal height of surface (= MSS + F + T)

N: Geoid model ... from satellite and terrestrial gravity

MDT: Mean Ocean Dynamic Topography

T: Tides

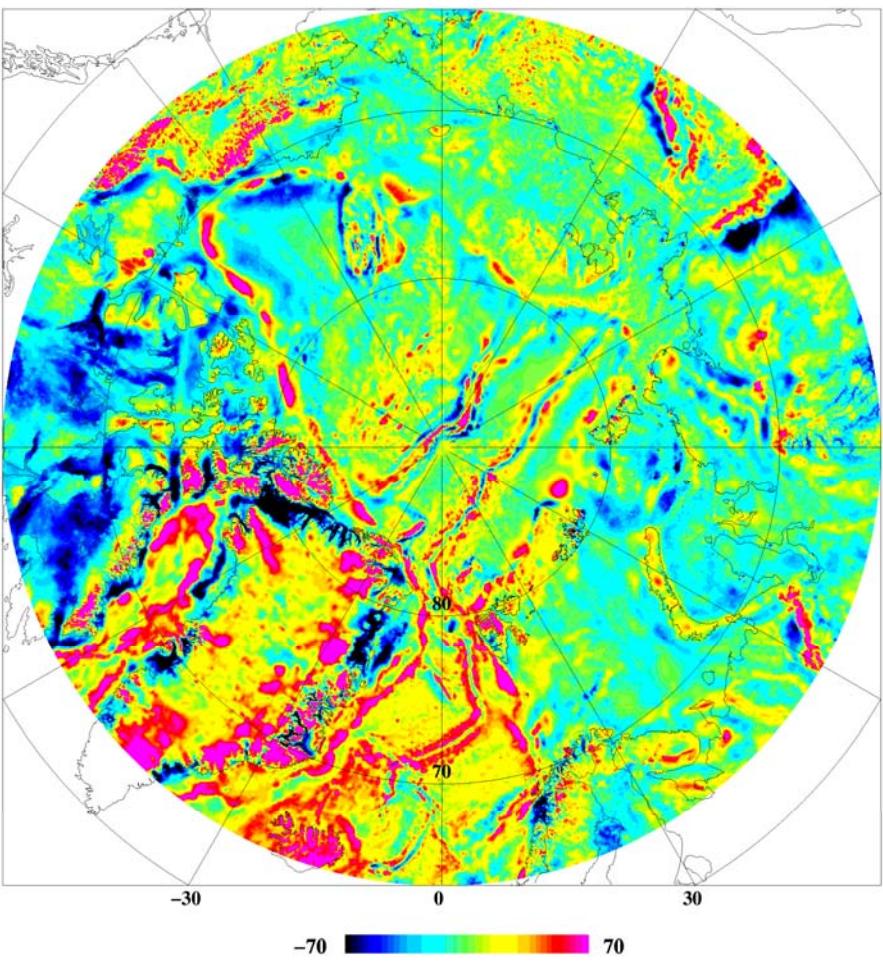
F: Sea-ice freeboard ( $\approx 6^*T$ )

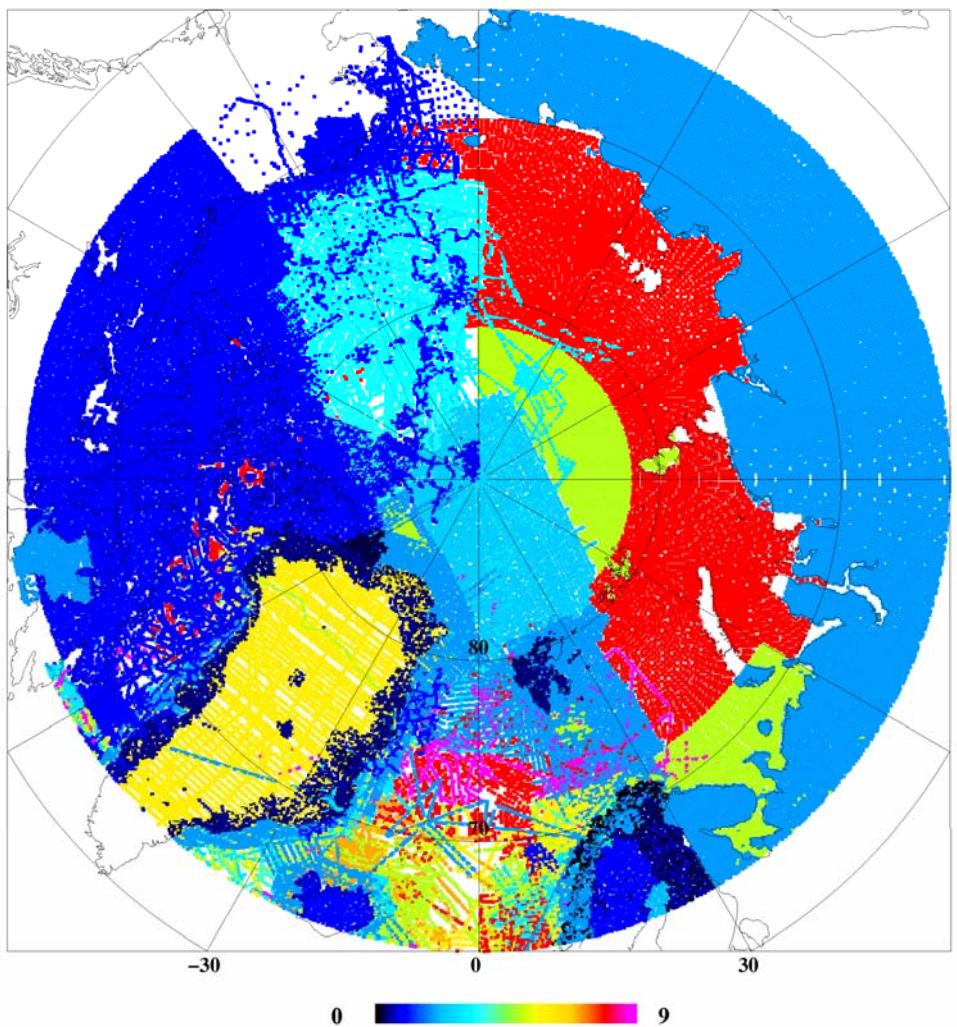




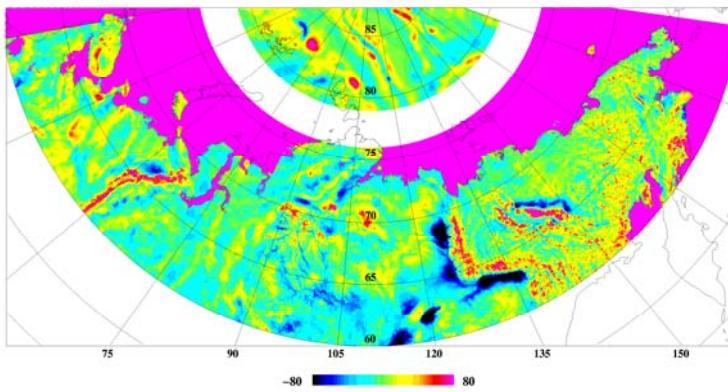
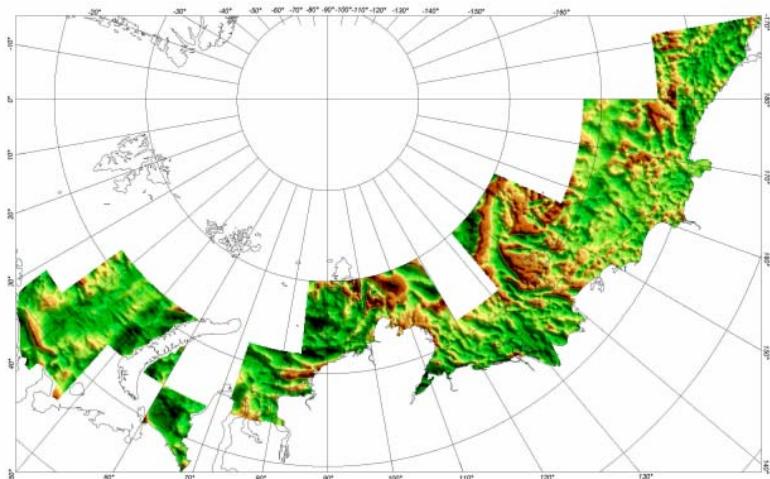
## The Arctic Ocean gravity field

- Arctic Gravity Project 2002 first grid
- 2006 update (ESA ArcGICE project):
  - GRACE data
  - New surface data (Russia, Alaska ..)
  - ICESat-derived gravity patches
- 2008 update
  - Better GRACE
  - New altimetry
  - More data
  - Incorporated in EGM08





## ArcGP data sources





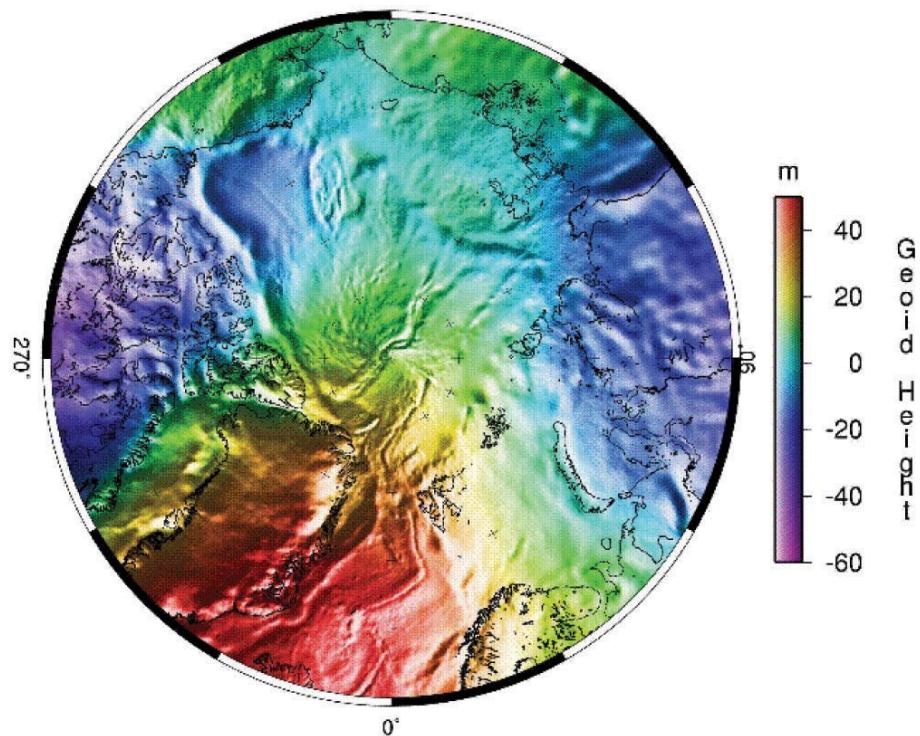
## Geoid of the Arctic from ArcGP and GRACE

*Method:*

- Remove reference field spherical harmonics expansion
- Stokes integral on residuals, spectrally band-limited (Wong-Gore modified Stokes' kernel)

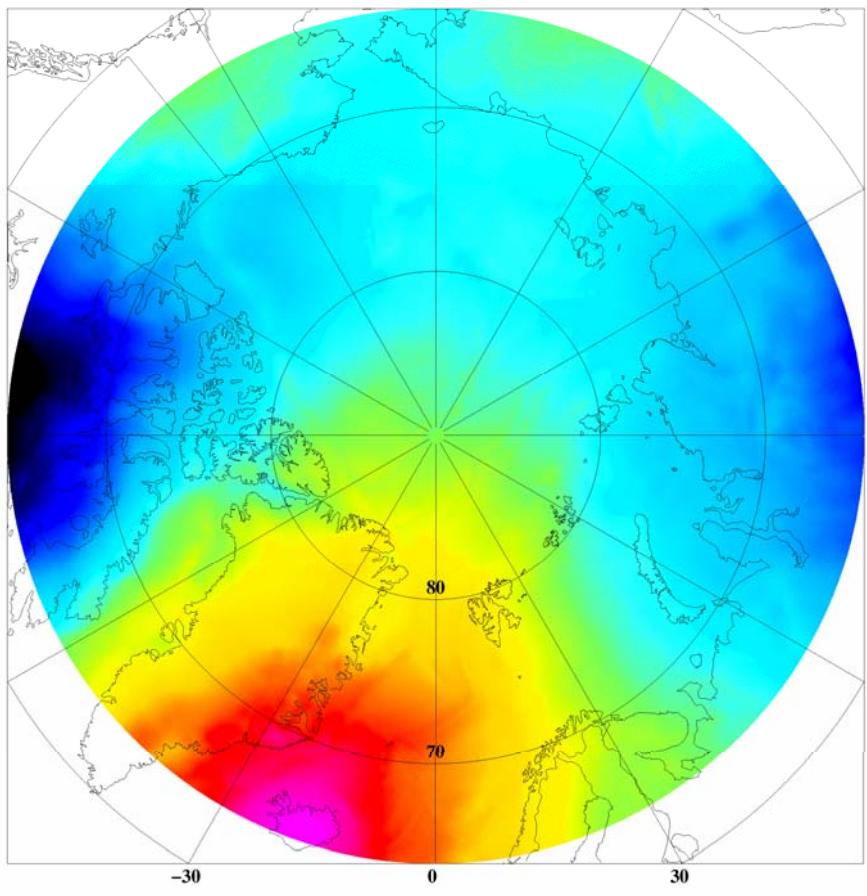
$$N = \frac{R}{4\pi G} \iint_{\sigma} \Delta g S'(\psi) d\sigma \quad S'(\psi) = \sum_{l=N}^{\infty} \frac{2l+1}{l-1} w_l P_l(\cos \psi)$$

- Stokes' integral by spherical FFT
- Restore reference field => final geoid
- Formal error estimates by collocation



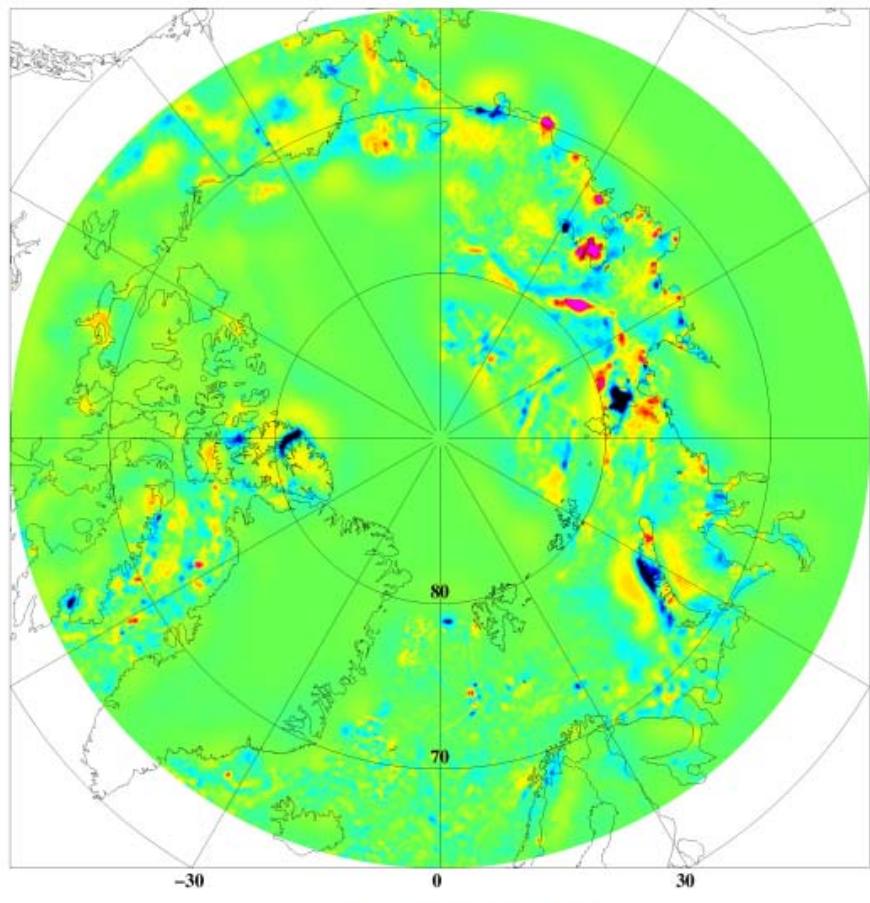


**2006 ArcGP geoid (m)**



-40     70

**Difference 2008-2006 geoid (cm)**

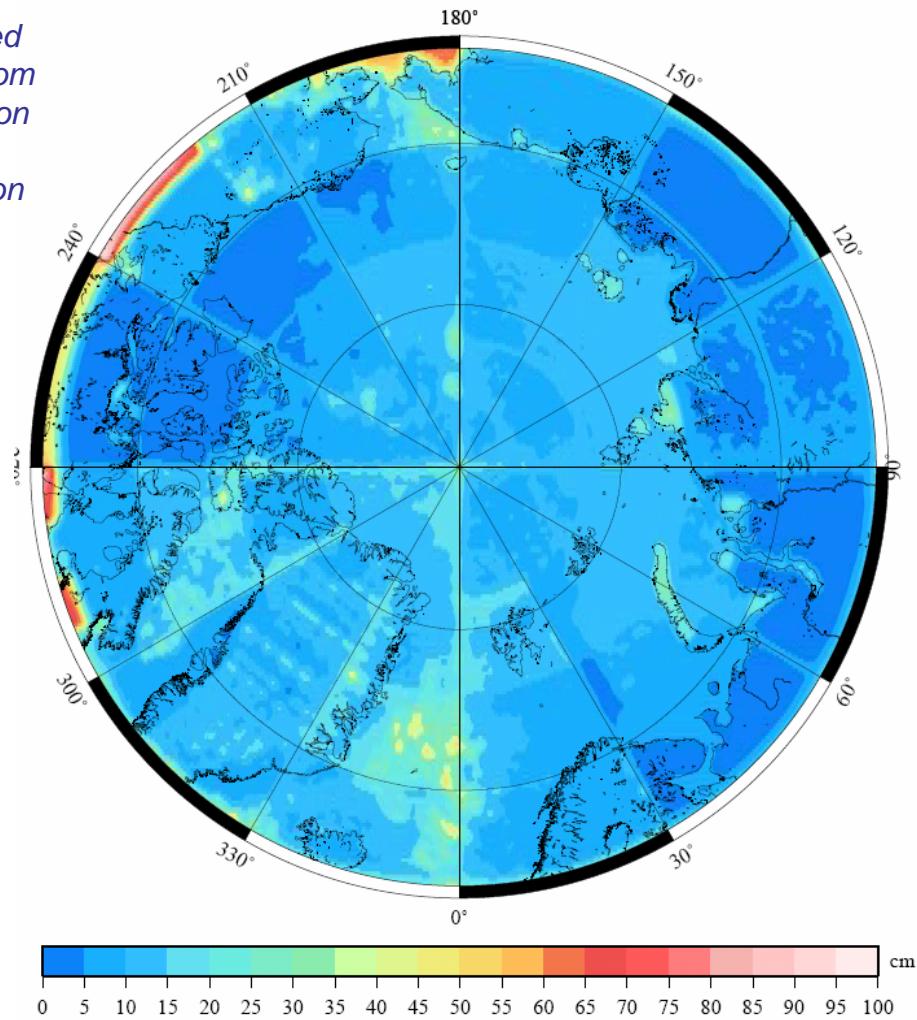


-50     50

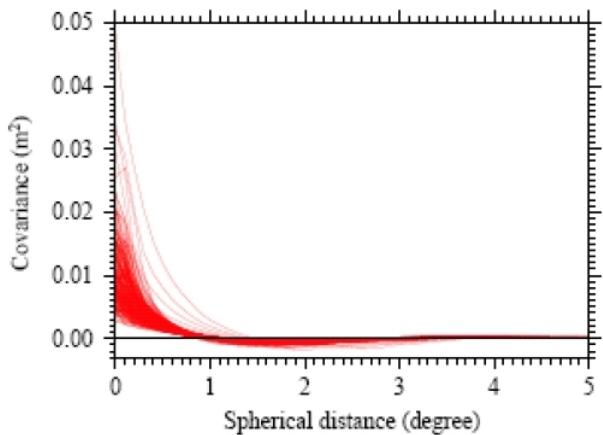


## Error estimate of ArcGP geoid (2006 version – ESA ArcGICE study)

*Estimated errors from collocation optimal estimation*



*Error covariance ensemble along meridians*





## MSS and MDT from ICESat

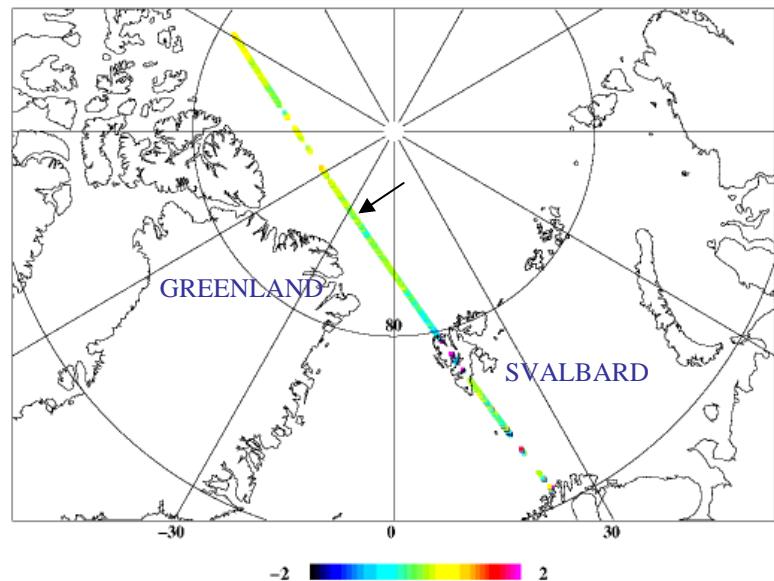
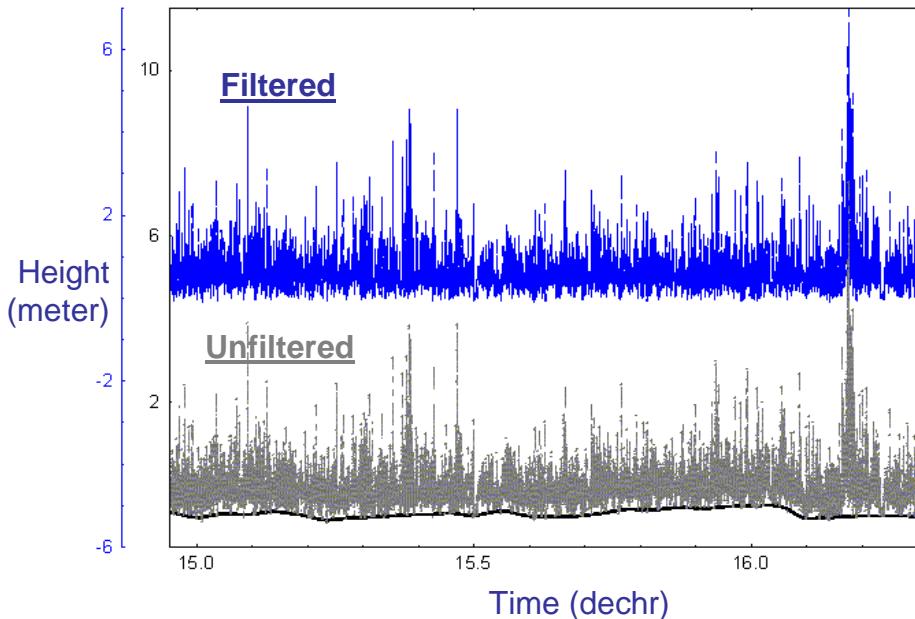
This study – January 2009:

- 14 ICESat periods, release 28 (March 2003 – March 2008)
- TPX tidal models, No IB
- Along-track lowest level filtering for sea ice
- Ice freeboard gridded and smoothed
- MDT = SSH – geoid – freeboard height

	ICESAT periods		
	FEB-MAR	JUN	OCT-NOV
2003:	L1A	-	L2A
2004:	L2B	L2C	L3A
2005:	L3B	L3C	L3D
2006:	L3E	L3F	L3G
2007:	L3H	-	L3I
2008:	L3J		

(r.i.p.)

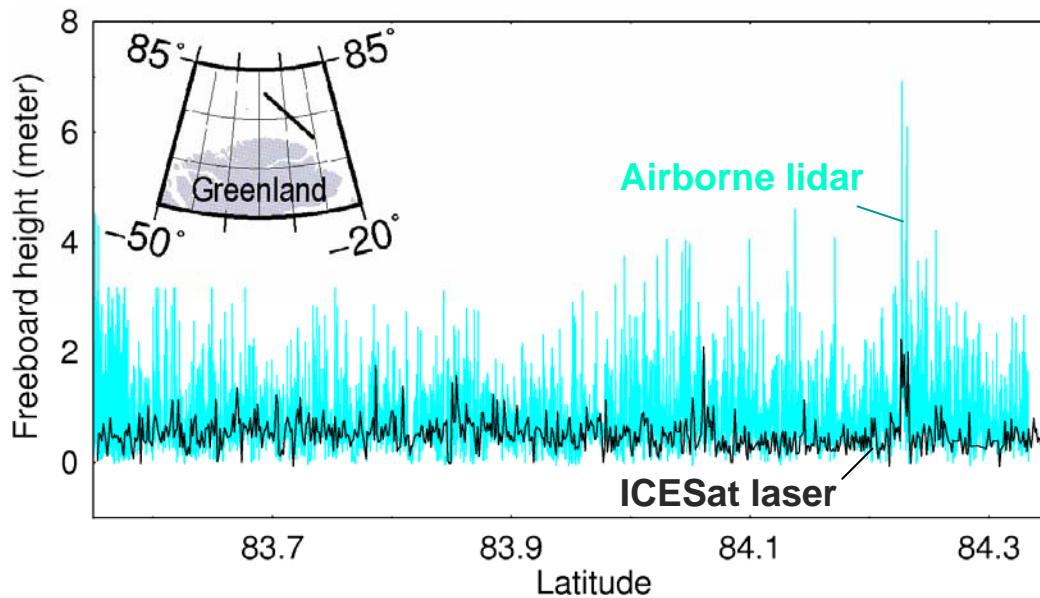
Lowest-level filtering: airborne lidar N of Greenland



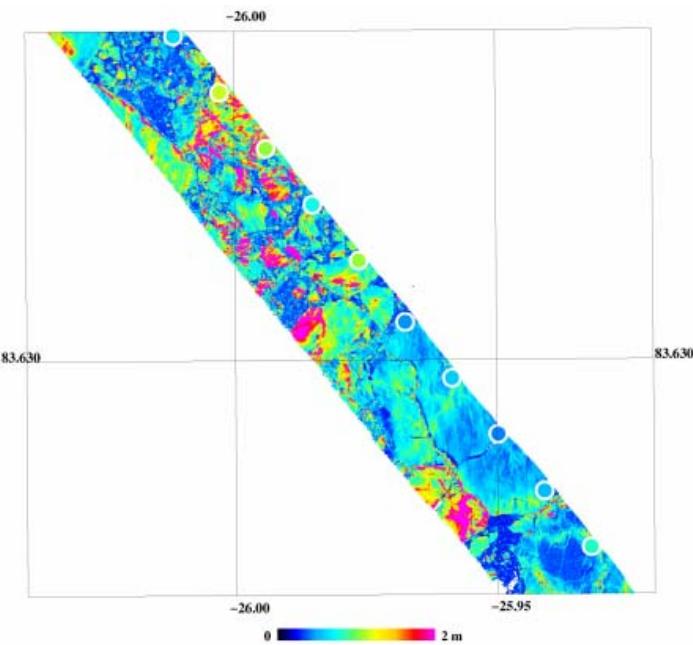


## Airborne lidar underflight of ICESat (May 2004)

- ICESat tend to underestimate sea-ice freeboard due to footprint size ..
  - bias 25 cm N of Greenland [DTU], 9 cm N of Alaska [NASA P3] ..
- Complicates determination of "absolute" MDT



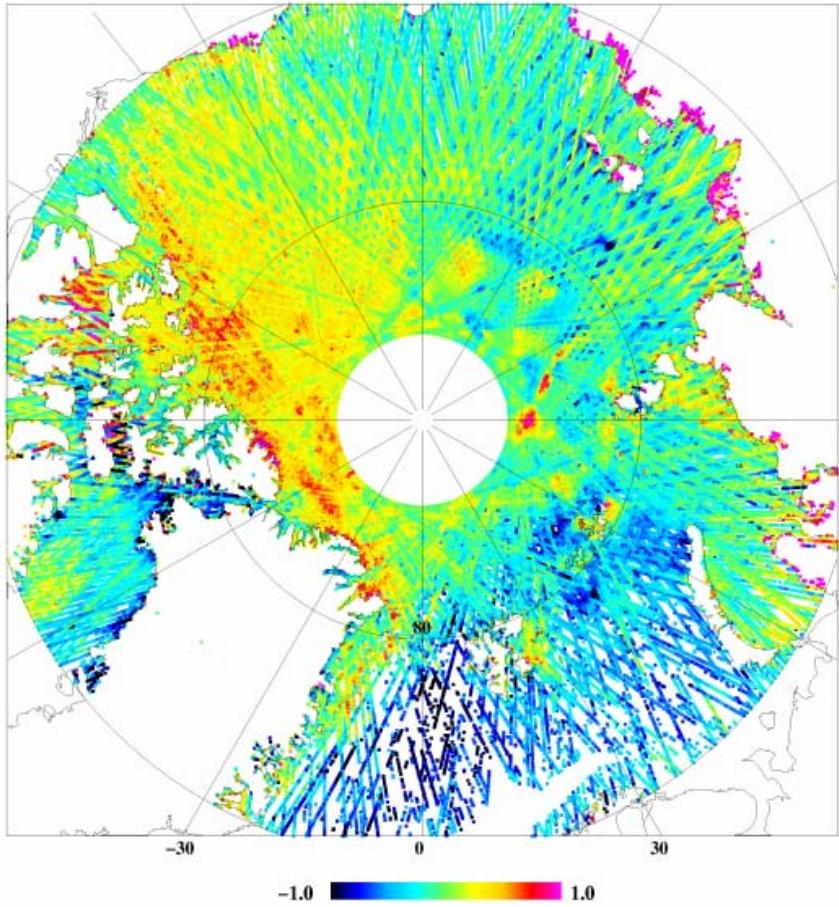
Laser swath scan and ICESat footprints



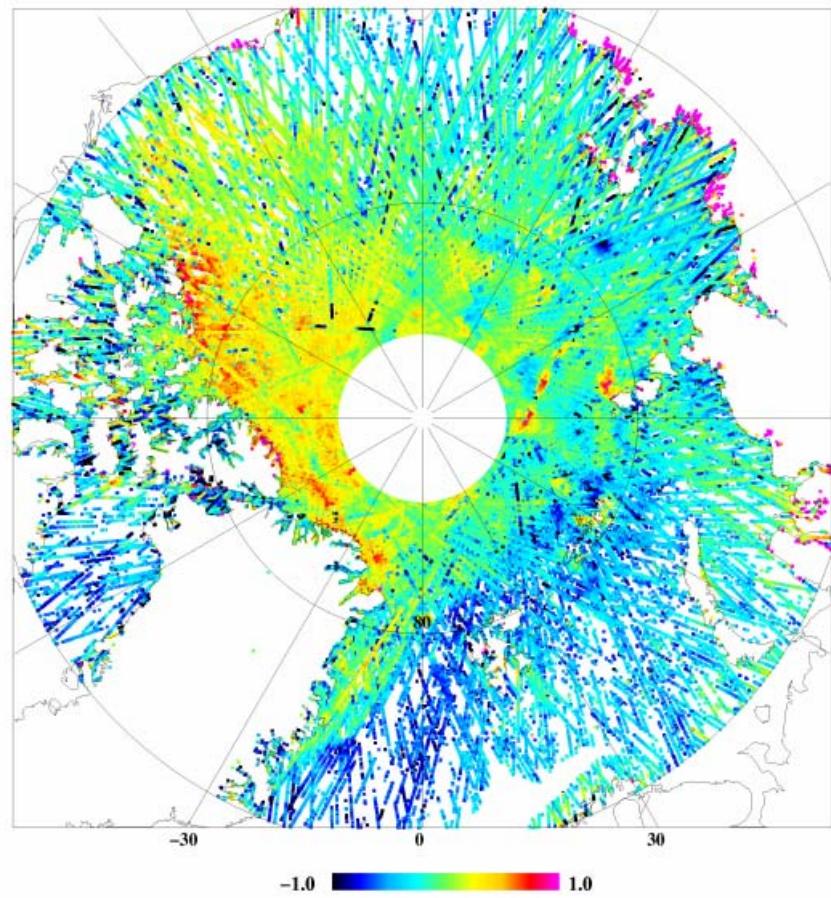


## New study: ICESat SSH – ArcGP v2 geoid examples

L2B – Feb/Mar 04



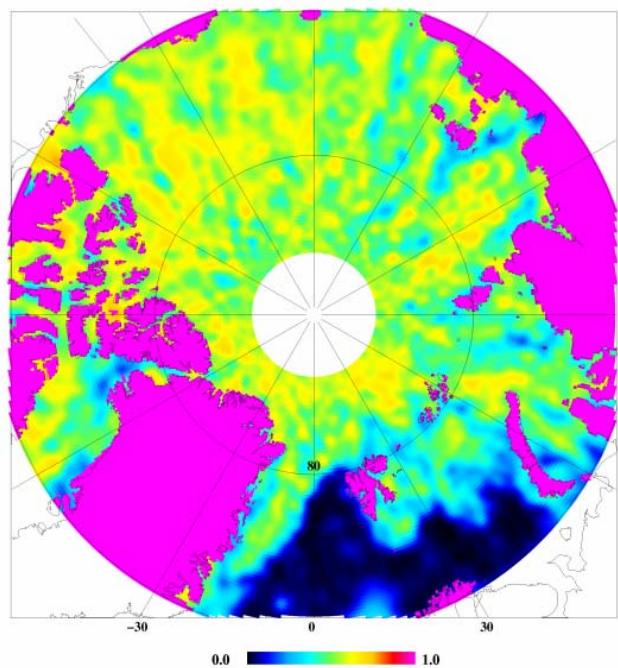
L3A – Oct/Nov 04



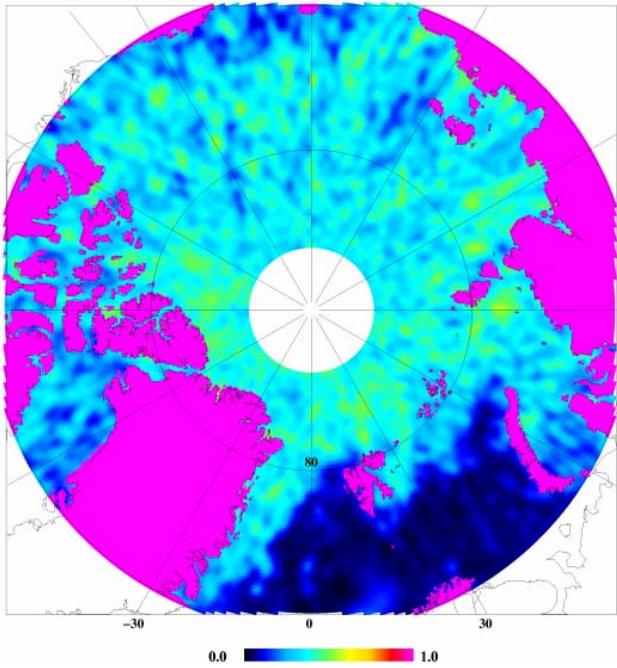


## Reflectivity outlines ice edge

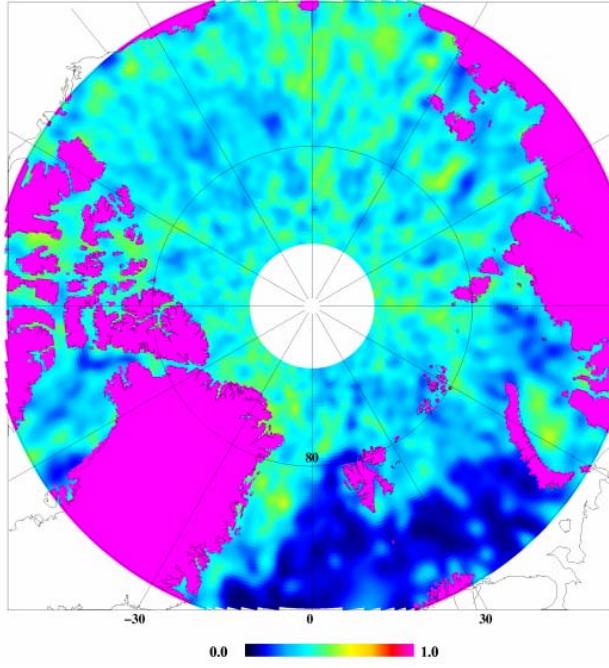
L1A - Mar 03



L2A - Oct 03



L2C - Jun 04

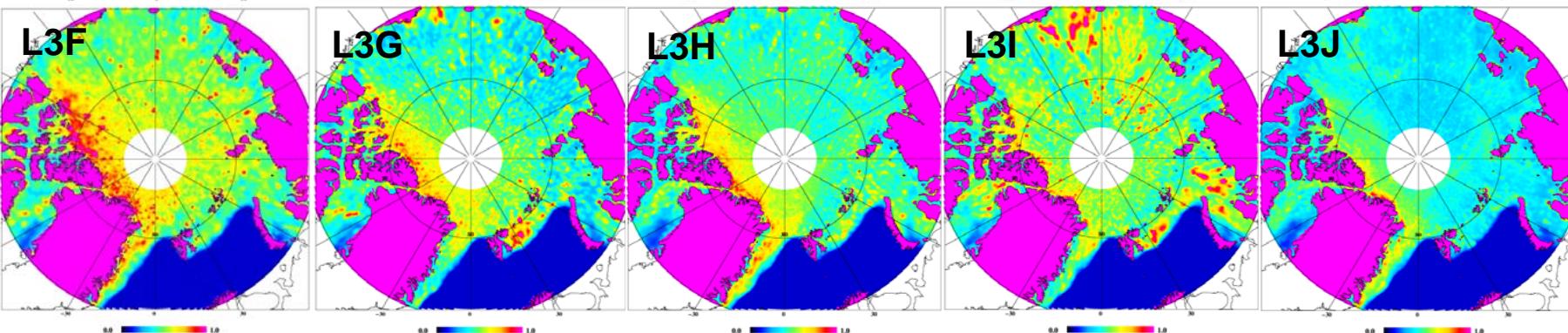
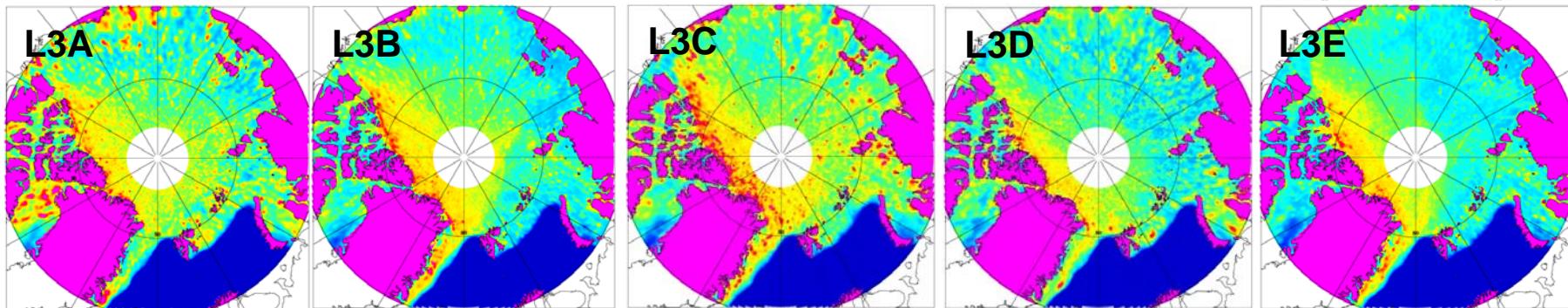
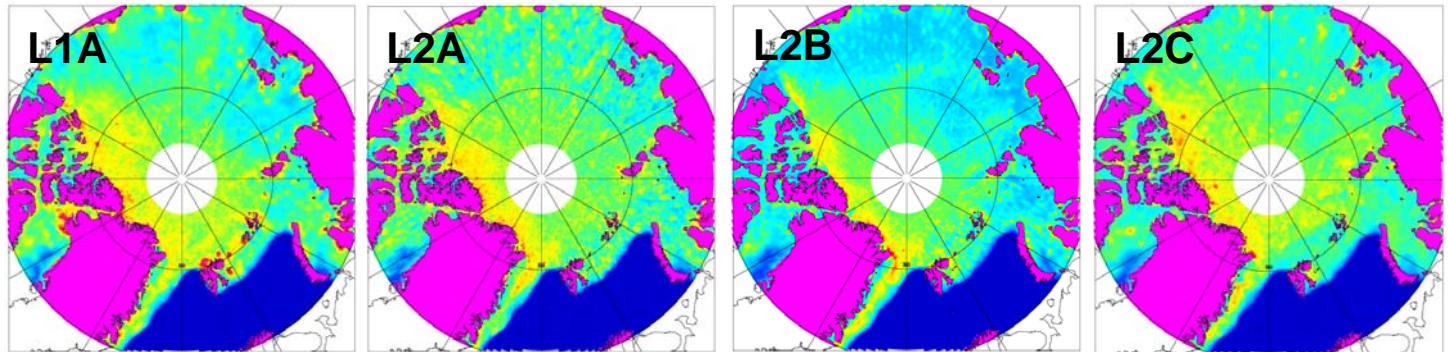




## Sea-ice freeboard heights from ICESat

Feb/Mar 2003 –  
Feb/Mar 2008  
(North Atlantic  
masked by  
a reflectivity)

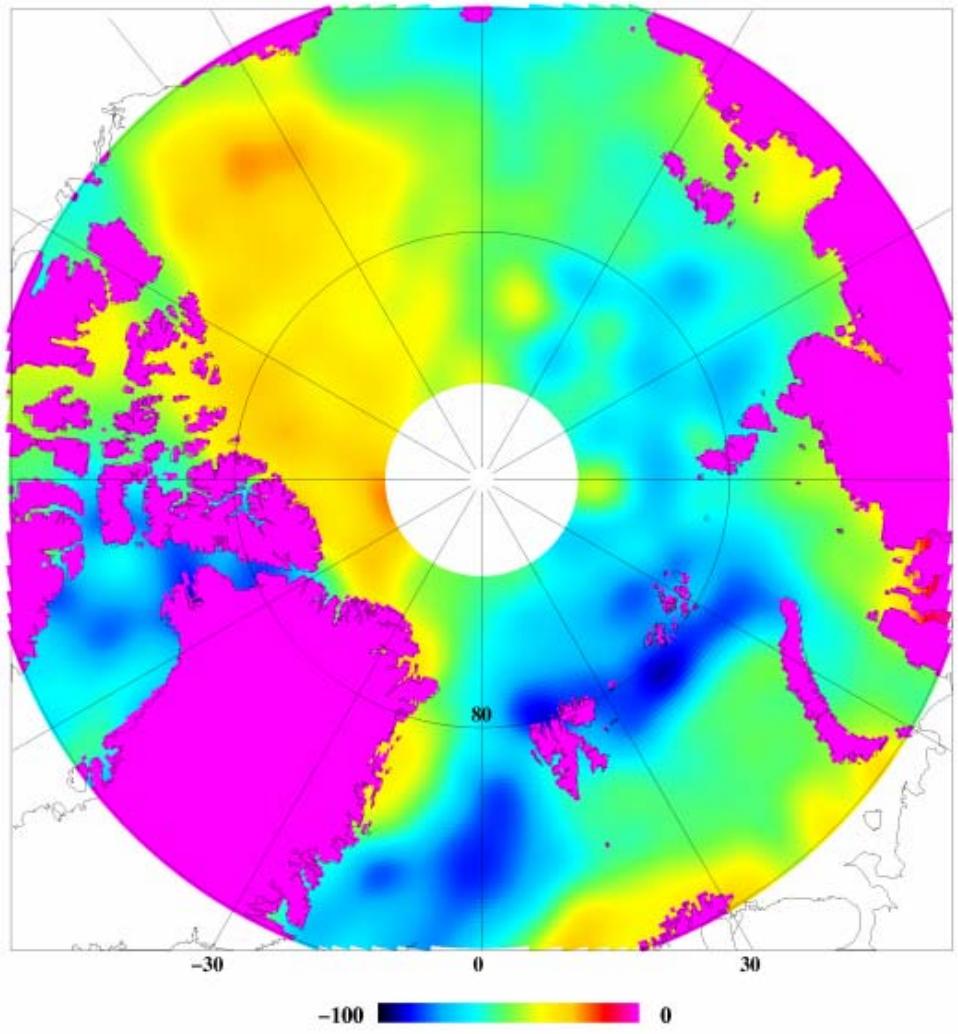
Colour scale 0 – 1 m



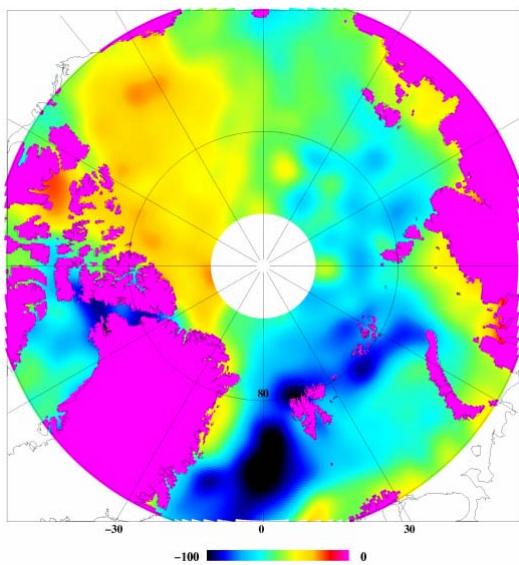


## MDT from ICESAT alone March 2003-8 (L1A-L3J)

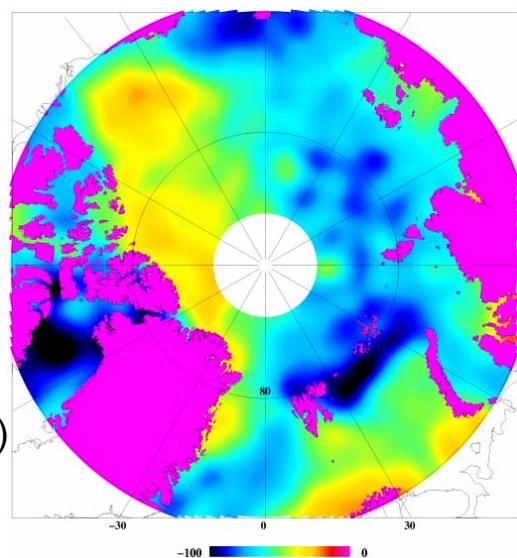
Average 2003-8 (14 periods)



March  
average  
(6 per.)



October  
average  
(5 periods)

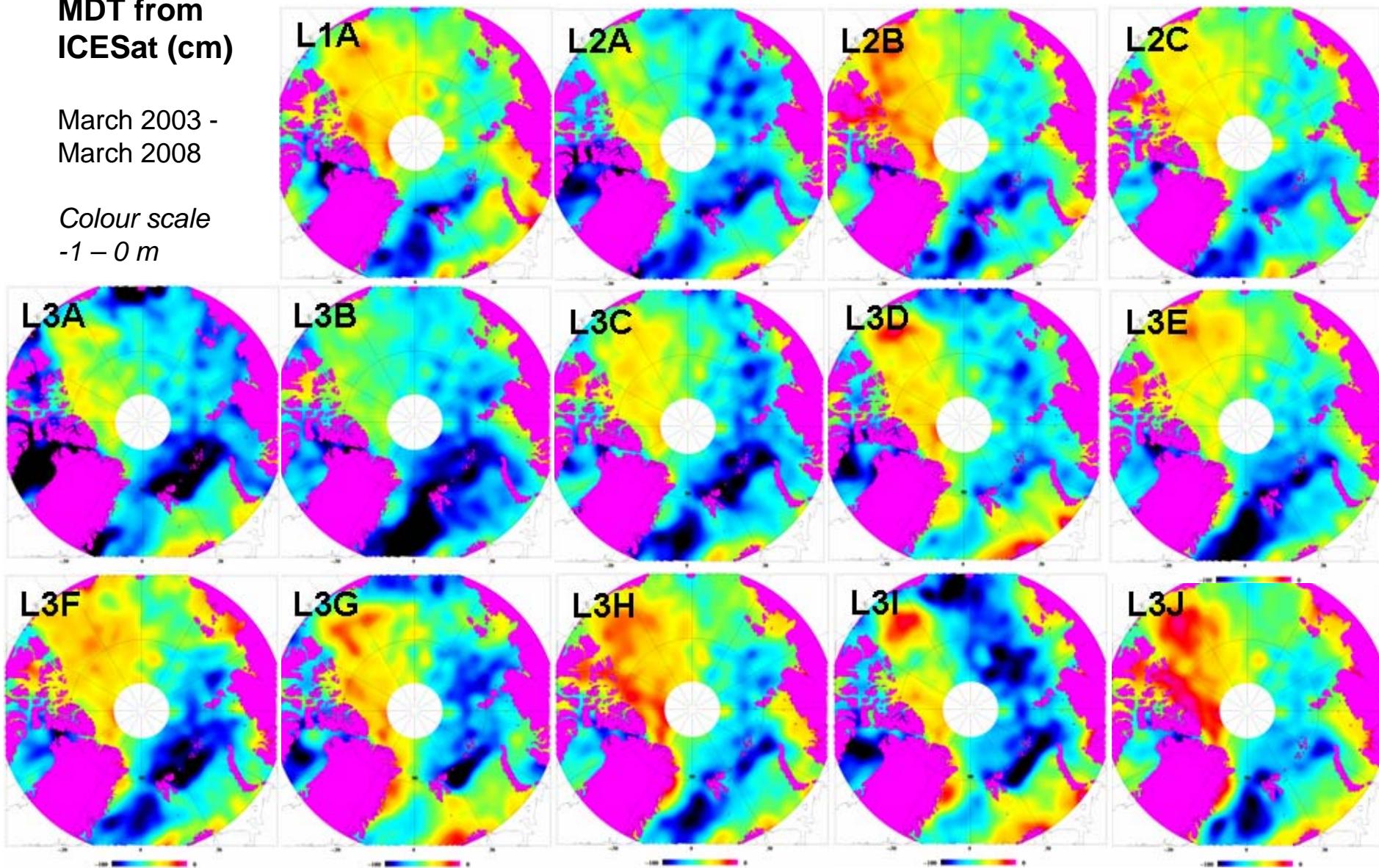




MDT from  
ICESat (cm)

March 2003 -  
March 2008

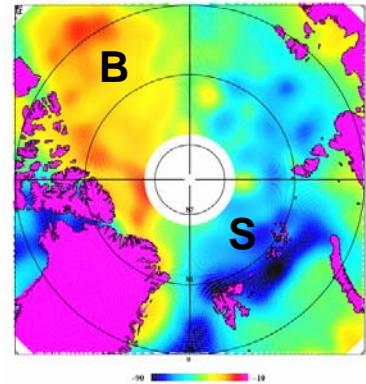
Colour scale  
-1 – 0 m



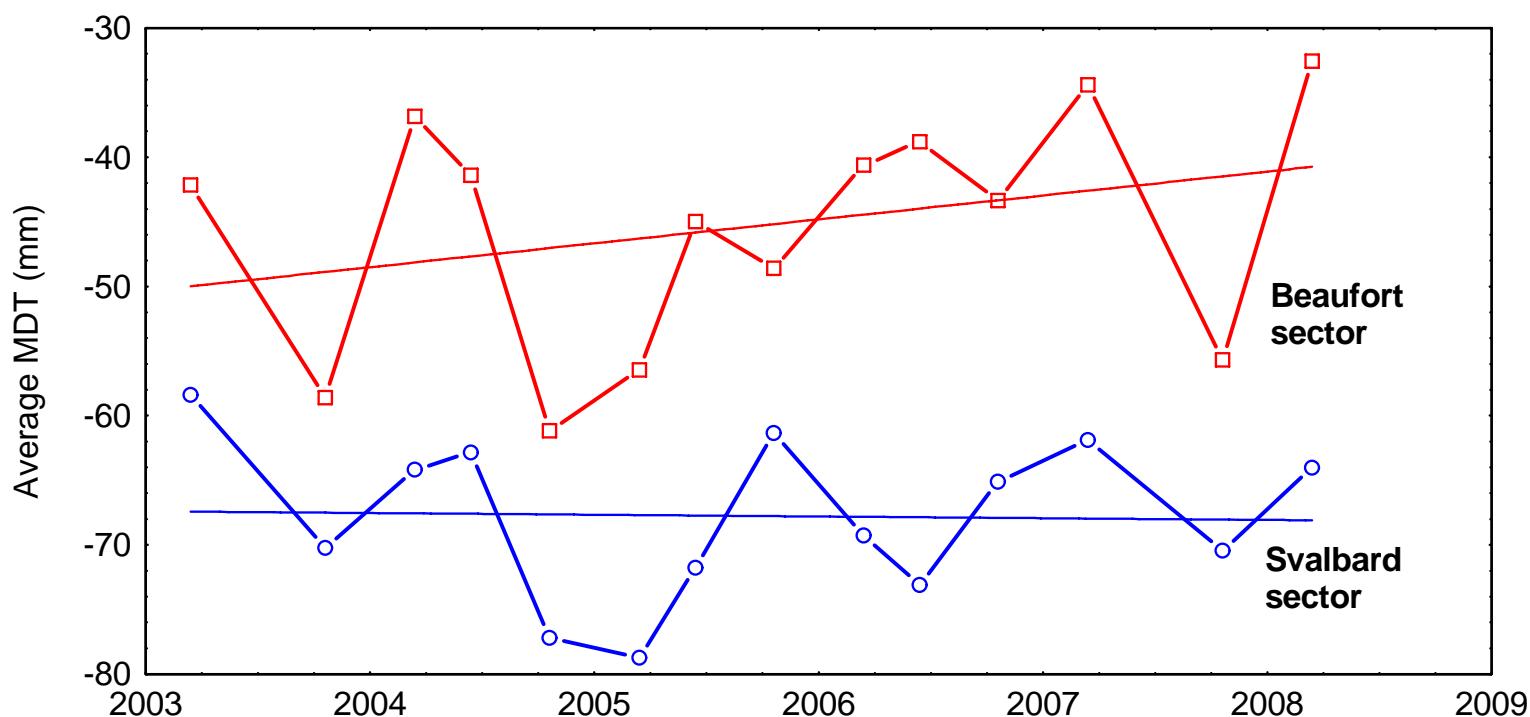


## Trend in MDT – as a function of time

- Slightly increasing difference in MDT from Svalbard sector (S) to Beaufort sector (B)
- Annual signatures, but not very clear



Average in 6 x 90 deg blocks





## MSS application: MDT estimation - "remote sensing" (ICESat/ArcGP) vs. oceanography

$$MDT = MSS - N$$

<i>MDT Model</i>	<i>Resolution in Arctic</i>	<i>Atmospheric Forcing</i>
MICOM	40 km	NCEP/NCAR
OCCAM	$\frac{1}{4} \times \frac{1}{4}$ deg	ECMWF
PIPS (W. Maslowski)	9 km	ECMWF
Univ. Wash. (M. Steele)	40 km	NCEP/NCAR

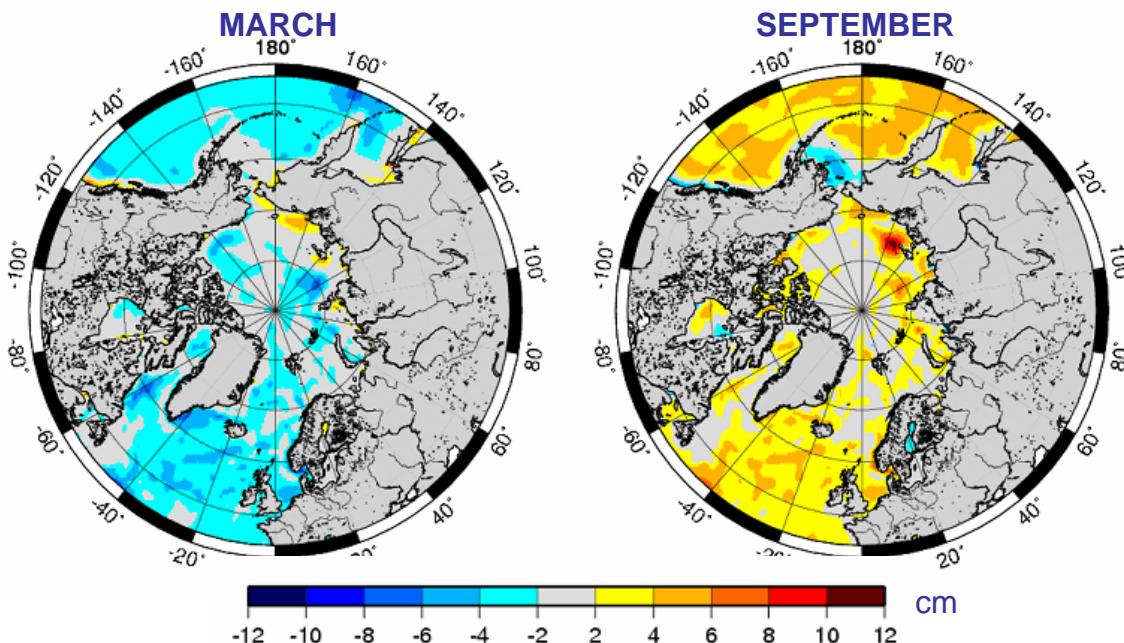
**Example: New MICOM run  
(Nansen Center, Norway)**

New Global Model,  $2.4^\circ \times \cos \varphi$   
resolution

1948-2005 (3xNCEP)

1958-2001 (5-10xERA)

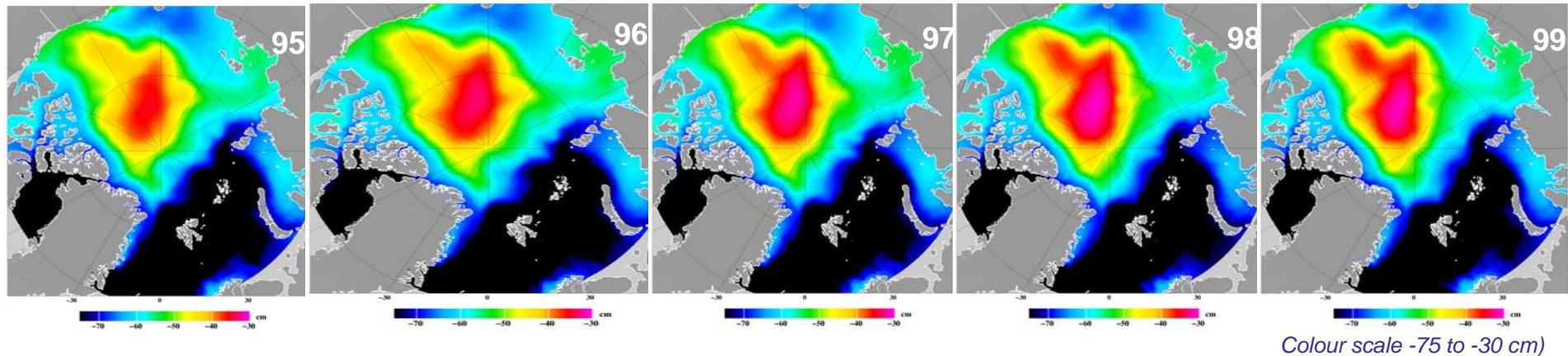
MDT mean for 1948-2005  
(NCEP), 1958-2001 (ERA) +  
anomalies March/September





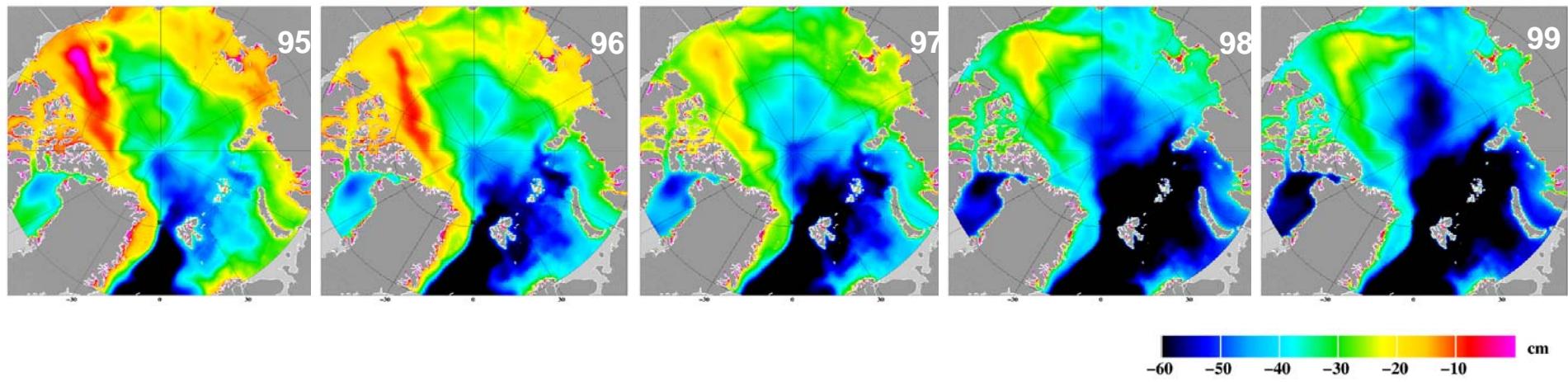
## MDT: OCCAM interannual variability 1995-1999

Old model (ArcGICE)



Colour scale -75 to -30 cm)

Newer model



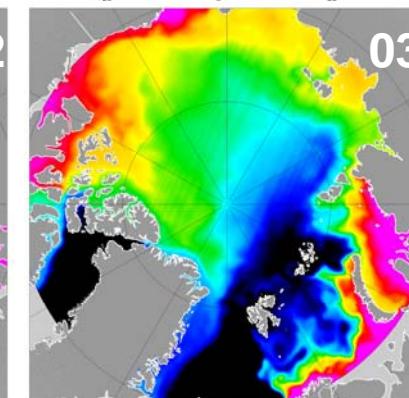
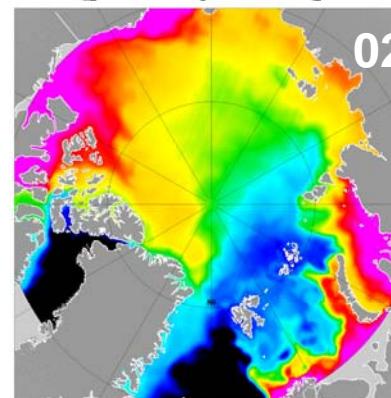
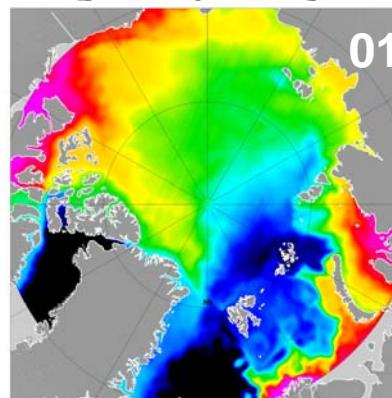
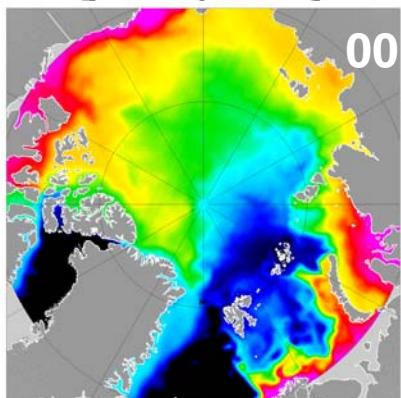
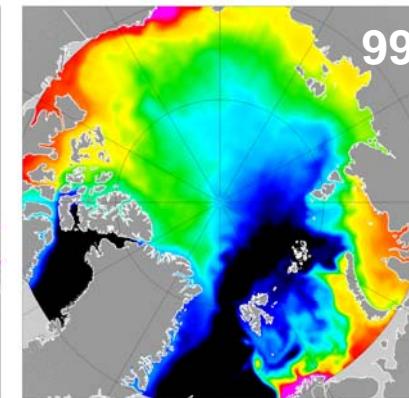
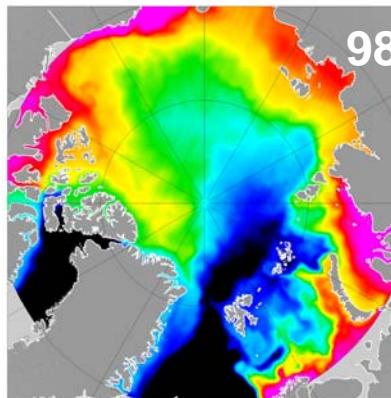
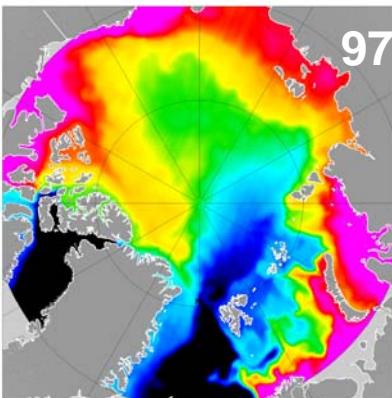
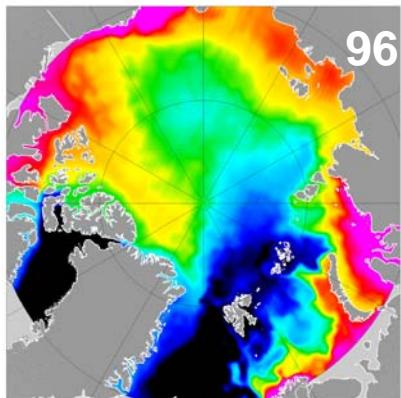
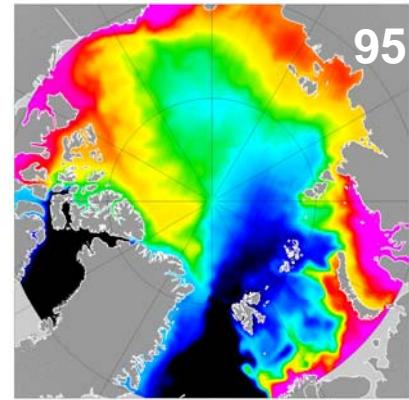
Courtesy: UK Oceanographic Center in Southampton



## MDT: PIPS interannual variability March 1995-2003

Courtesy: W. Maslowski, Naval Postgraduate School

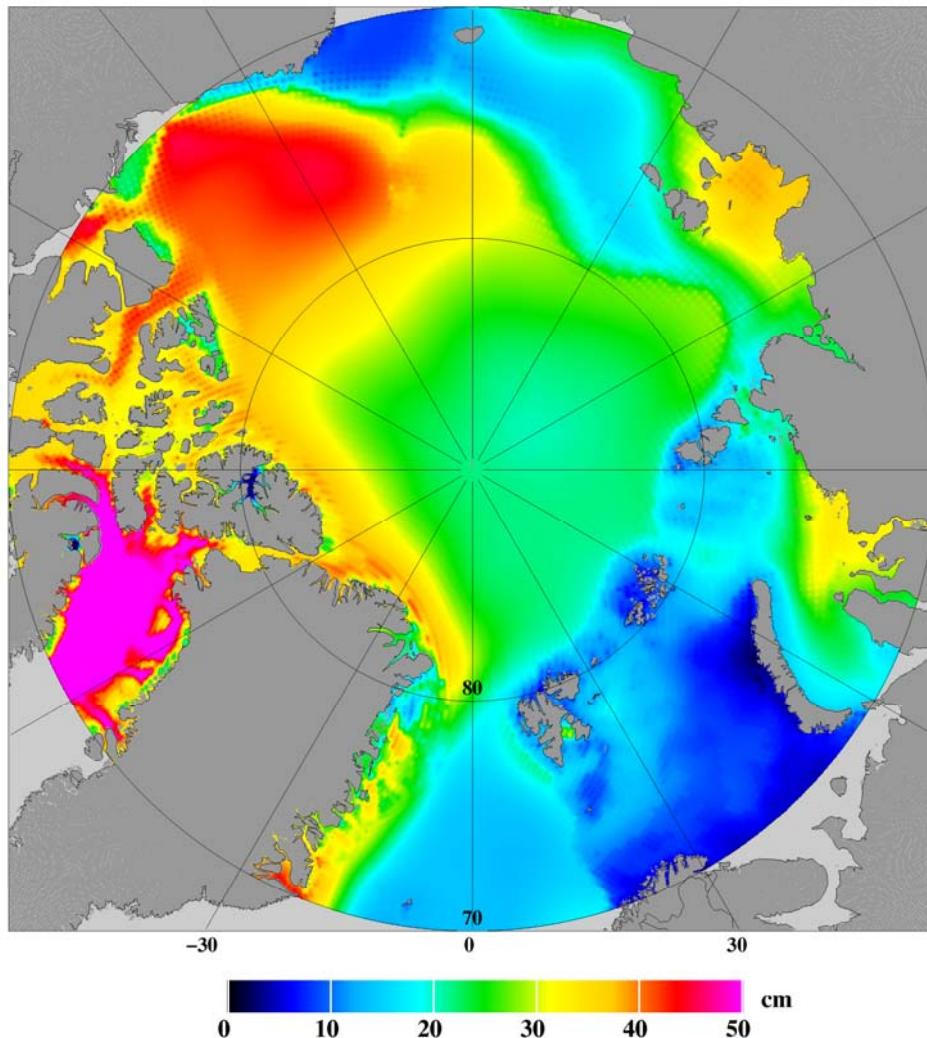
Colour scale -30 to 0 cm



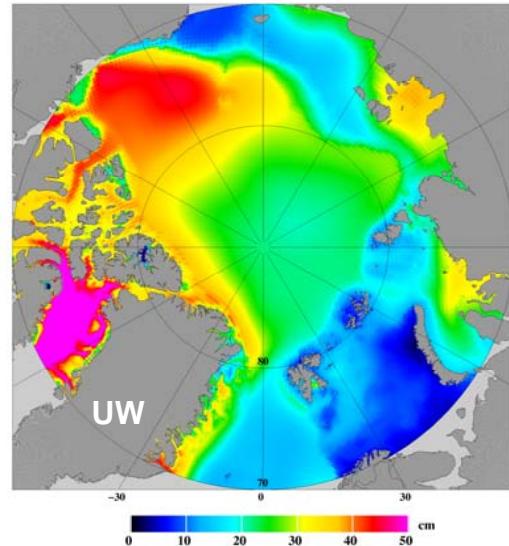
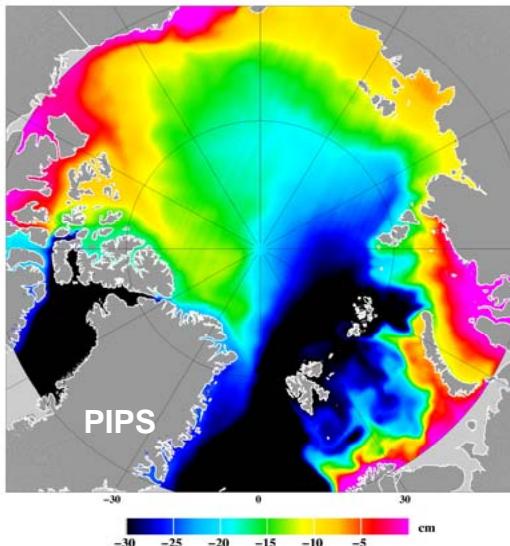
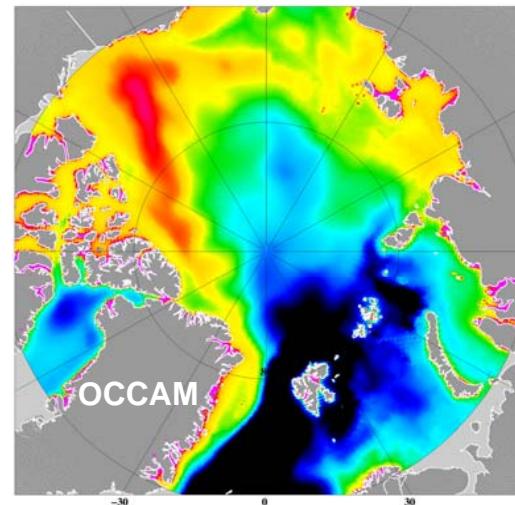
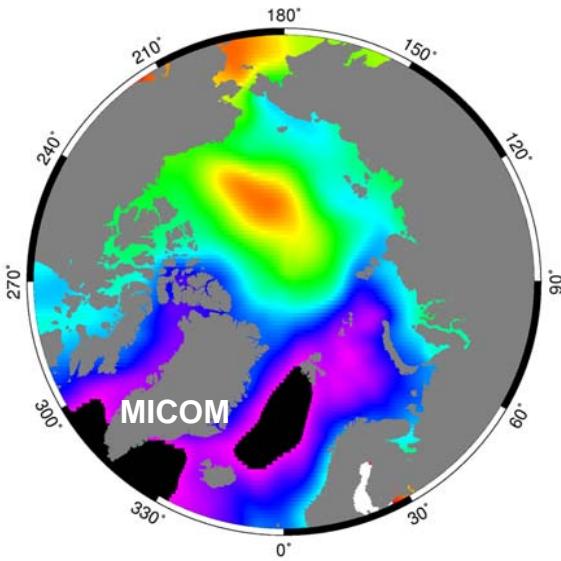
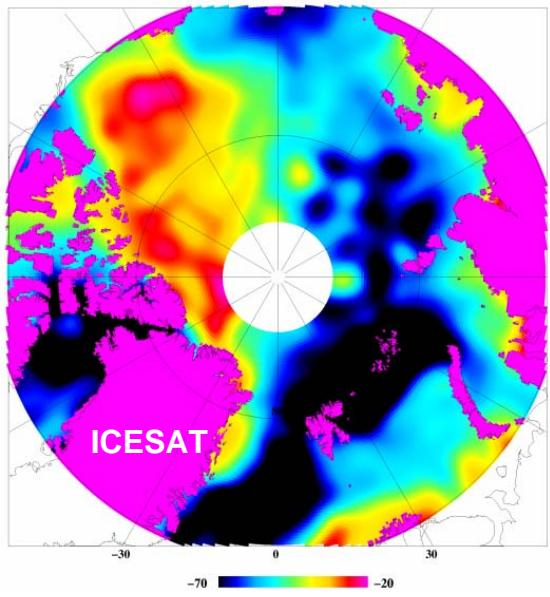
-30 -25 -20 -15 -10 -5 cm



## MDT: UW average 1955-2006



Courtesy: M. Steele, University of Washington



## Intercomparison of mean MDT from "remote sensing" (ICESat/GRACE) and oceanographic models

(colour scale ranges ~50 cm)



## Conclusions

- New ArcGP geoid incorporating new data and GRACE
- ICESat provides Arctic Ocean realistic MSS and sea-ice free-board heights
  - *ICESAT MSS may expand 8-year ERS MSS to 86°N – seasonal changes seen*
- MDT determined from ICESat+ERS MSS and GRACE/ArcGP geoid agrees qualitatively well with oceanographic models ..
  - *Large difference between oceanographic models ..*

*CryoSat and GOCE will significantly improve determination of MDT*





**Thanks for the attention**

**Greenland workshops, Nuuk AUG 25-27, 2009:**

- Changes of the Greenland Cryosphere
  - Arctic Freshwater Budget (FreshNor)
- see [www.space.dtu.dk/nuuk2009](http://www.space.dtu.dk/nuuk2009)

DTU Space  
National Space Institute



ARCTIC TECHNOLOGY CENTER



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